#### ARTICLE

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# Automated hydrodynamic modelling of a complex between a human IgE fragment (Fc $\varepsilon$ 3-4) and the IgE high affinity receptor Fc $\varepsilon$ RI $\alpha$ -chain

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**Abstract** The binding of IgE to its high affinity receptor Fc $\varepsilon$ RI plays an important role in the allergic response. The interaction between soluble  $Fc \in RI\alpha$ -chain ( $sFc \in RI\alpha$ ) and Fc $\varepsilon$ 3–4, a fragment of IgE consisting of the C $\varepsilon$ 3 and C $\varepsilon$ 4 heavy chain constant domains, has been studied using analytical ultracentrifugation (Keown et al. this volume). Here we describe the development of a simple automated hydrodynamic modelling technique and its application to this interaction. This procedure utilises sphere models of the two molecules and performs an automated systematic translational search of sFc $\varepsilon$ RI $\alpha$  relative to Fc $\varepsilon$ 3–4. The result of this is the generation of 40,359 individual models of how the receptor can be placed relative to Fc $\varepsilon$ 3–4. These are then assessed for consistency by comparing the sedimentation coefficients generated for the models to the experimentally determined sedimentation coefficients, and are displayed graphically to show allowed and disallowed complexes. From this analysis, it is clear that the complex between sFc $\varepsilon$ RI $\alpha$  and Fc $\varepsilon$ 3-4 is compact, with the most elongated models being excluded. In addition, sFc $\varepsilon$ RI $\alpha$ appears not to interact with the C-terminal end of Fc $\varepsilon$ 3–4, and probably binds either to the sides or face, observations which are consistent with other experimental data on the Fc $\varepsilon$ RI $\alpha$ /IgE interaction. Automated hydrodynamic modelling also has the potential to be used for other interactions, providing a simple way of looking at a large number of models, and making rigorous studies of interacting components more feasible.

**Key words**  $Fc \in RI \cdot IgE \cdot Analytical ultracentrifuge \cdot Automated hydrodynamic modelling$ 

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#### Introduction

The affinity of IgE for its high affinity cell-surface receptor  $Fc \varepsilon RI$  ( $K_a = 10^{10} \ M^{-1}$ ) is more than an order of magnitude greater than that for antibodies of any other class with any known Fc receptor (Ravetch and Kinet 1991). The stability of the interaction may be inseparable from the role of IgE in immediate hypersensitivity reactions and fortuitously makes it amenable to study by hydrodynamic methods. IgE binds through its Fc portion to  $Fc\varepsilon RI$  on mast cells and basophils, and when this receptor-bound IgE is crosslinked by multivalent antigen, it results in the release of inflammatory mediators, and immediate type I hypersensitivity. Consequently, studies on the IgE-receptor complex yield information important for developing strategies to combat allergic reactions, such as peptides which inhibit IgE-Fc $\varepsilon RI$  binding specifically (McDonnell et al. 1996).

FceRI is made up of four chains  $(\alpha, \beta, \gamma_2)$ , but the extracellular portion of the  $\alpha$ -chain, comprising two single immunoglobulin-like domains, is sufficient to generate full binding affinity (Hakimi et al. 1990; Blank et al. 1991). The binding sites have been mapped to Ce3 in the IgE-Fc (Helm et al. 1988; Nissim and Eshhar 1992; Basu et al. 1993; reviewed in Sutton and Gould 1993 and Beavil et al. 1993), and to the second, membrane-proximal immunoglobulin-like domain,  $\alpha_2$ , in the  $\alpha$ -chain (Nissim and Eshhar 1992; Basu et al. 1993; Robertson 1993; Scarselli et al. 1993; reviewed in Hulett and Hogarth 1994).

Although the binding sites in IgE and Fc $\varepsilon$ RI are roughly defined, little is known about the arrangement of the two ligands in the complex. Using recombinant IgE-Fc and a soluble recombinant fragment of Fc $\varepsilon$ RI  $\alpha$ -chain (sFc $\varepsilon$ RI $\alpha$ ) containing the two immunoglobulin-like domains, we have, in a previous study, been able to determine both the stoichiometry of the complex and its approximate shape in free solution (Keown et al. 1995). The stoichiometry of binding is 1:1, and it appears that possible modes of binding are restricted to those in which there is considerable overlap of the immunoglobulin domains. The hydrodynamic modelling carried out in that study was relatively

crude, since only 20-30 models representing limiting forms of the complex were examined. In addition, the bend in IgE-Fc was not well characterised, which constrained the interpretation of the models. Even now, the range of possible modes of bending envisaged for IgE-Fc (Beavil et al. 1995) would lead to an impossibly large number of models of the complex. Hence, we have studied the complex formed between sFc $\varepsilon$ RI $\alpha$  and a smaller recombinant fragment of IgE (Fc $\varepsilon$ 3–4) which contains only the C $\varepsilon$ 3 and C $\varepsilon$ 4 domains and is therefore unlikely to be bent. We have also attempted to refine the hydrodynamic model of the Fc $\varepsilon$ 3–4/sFc $\varepsilon$ RI $\alpha$  complex by introducing an automatic procedure to generate many thousands of models representing different orientations of the complex. This is analogous to the AUTOSCT procedure for modelling small angle scattering data, previously described in Beavil et al. (1995).

## **Materials and methods**

## Sedimentation velocity studies

Protein samples were a kind gift of M. Keown (Keown et al., this volume). Sedimentation velocity experiments were performed at 20.0 °C using the Beckman Optima XL-A centrifuge with an An60 Ti rotor at speeds from 40,000 rpm to 50,000 rpm for both  $Fc\varepsilon3-4$  and its complex with  $sFc\varepsilon RI\alpha$ . The sedimentation coefficient for  $sFc\varepsilon RI\alpha$  was previously determined (Keown et al. 1995). Protein concentrations corresponded to  $A_{280}$  in the range 0.5-0.8. Data were acquired as absorbance measurements at a wavelength of 280 nm and a radial spacing of 0.003 cm and analysed with the program XLAVEL (Beckman) to yield the uncorrected sedimentation coefficient. Data were collected at three concentrations, s was extrapolated to zero concentration, and then corrected to obtain  $s_{20,w}^0$  as previously described for IgE-Fc (Keown et al. 1995).

# Determination of hydrodynamic parameters

The partial specific volume, relative molecular mass and volume of recombinant IgE-Fc and  $sFc\epsilon RI\alpha$  were calculated from the amino acid compositions, together with estimated carbohydrate contents (Perkins 1986), and are shown in Table 1. The sedimentation coefficients for the two components separate and when complexed were determined as described for IgE-Fc and  $sFc\epsilon RI-\alpha$  (Keown et al. 1995).

**Table 1** Composition data for  $Fc\varepsilon 3-4$ ,  $sFc\varepsilon RI\alpha$  and their complex

	M <sub>r</sub>	$\overline{v}$ (cm <sup>3</sup> g <sup>-1</sup> )	Dry volume (nm <sup>3</sup> )	Dry model volume (nm³)
Fc $\varepsilon$ 3–4	02	0.728	66.9	63.6
sFc $\varepsilon$ RI $\alpha$		0.698	40.5	36.6
Complex		0.716	107.4	103.6

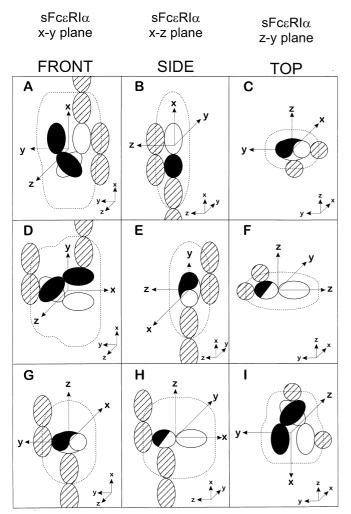
Generation of sphere models of Fc $\varepsilon$ 3–4, sFc $\varepsilon$ RI $\alpha$  and their complex

To calculate simulated hydrodynamic parameters, models made from small non-overlapping spheres were generated. These do not represent chemically defined subunits but are used only to approximate a simple structure. Crystal coordinates of either the whole protein structure or a single domain can be converted into a sphere model. In this case, model calculations of the sedimentation coefficients were based on the IgE-Fc models of Padlan and Davies (1986), and Helm et al. (1991), and on a model of sFc $\varepsilon$ RI $\alpha$  based on the crystal structure of CD2 (McDonnell et al. 1996; Beavil et al. 1993; Jones et al. 1992). Whilst a model of sFc $\varepsilon$ RI $\alpha$  by Padlan and Helm has been published (1992), it is currently unavailable in the Brookhaven Protein Data Bank, but it would not be expected to yield a significantly different sedimentation coefficient, as the methods used here are only sensitive to gross configuration. Unlike the case of IgE-Fc, the possibility that Fc $\varepsilon$ 3–4 could exhibit bending within the  $C\varepsilon 2$ – $C\varepsilon 3$  linker region does not have to be investigated, as the C $\varepsilon$ 2 domains are not present, and this simplifies the situation considerably. Carbohydrate chains were modelled on those found in the human Fc crystal structure (Deisenhofer 1981). These were attached to the putative carbohydrate sites on the proteins using Insight II molecular graphics software (Biosym Technologies, Inc.).

For calculations of the hydrodynamic models, the molecular models were first converted into spheres using a program BRKTOS in which the model was placed in a three dimensional grid of cubes (Smith et al. 1990; Perkins et al. 1993). The cubes were included as the building blocks of the hydrodynamic model if they contained at least one  $\alpha$ carbon atom. The dimensions of the cubes were optimised such that the total volume of the cubes equalled that of the dry protein volume calculated from the composition above (66.9 nm<sup>3</sup> and 40.5 nm<sup>3</sup> for Fc $\varepsilon$ 3–4 and sFc $\varepsilon$ RI $\alpha$ , respectively). The volumes were then increased to allow for a hydration shell, assumed to comprise 0.3 g of water/g glycoprotein and an electrostricted volume of 0.0245 nm<sup>3</sup> per bound water molecule (Perkins 1986; Smith et al. 1990; Perkins et al. 1993). The resulting models were assigned co-ordinates to produce the final hydrodynamic models based on non-overlapping spheres placed at the centre of each cube, which now had sides of 0.707 nm. Hydrodynamic calculations were performed by the modified Oseen tensor procedure using the program GENDIA (Garcia de la Torre 1977a, b, 1989). This method of generating sphere models is very crude but it has an interesting advantage over other methods in so far as it allows one to detect overlap between the two components of the complex by analysing the number of spheres or volume of the final model of the complex. We have also found that as expected, it is the volume excluded by the surface of the model which is important to the calculation of the frictional coefficients and not the volume of the spheres themselves.

Axis definitions for the components of the complex

The origin of  $Fc\varepsilon 3-4$  was set as a pseudoatom defined as the centre of mass of the molecule. Its x-axis was defined both by this pseudoatom and a second pseudoatom at the geometrical centre of residue 333 from the A and B chain, and the x-y plane was defined by the addition of a pseudoatom at the centre of mass of the A chain. The origin of  $sFc\varepsilon RI\alpha$  was initially set as a pseudoatom defined as the centre of mass of residues 100-176; its x-axis was defined both by this pseudoatom and a second pseudoatom at the centre of mass of residues 2-99; the x-y plane was defined by the addition of a pseudoatom at the centre of mass of the whole molecule. The origin was then translated to the centre of mass of the whole molecule (see Fig. 1).



**Fig. 1A–I** Schematic diagram of the Fcε3–4/sFcεRI $\alpha$  complex models. The two chains of Fcε3–4 are shown *shaded* and *open*, and sFcεRI $\alpha$  is *hatched*, with two of its many possible positions depicted in each panel. Models are viewed projected onto orthogonal planes defined by the axes of sFcεRI $\alpha$ . The x – y plane is the front view, x–z is the side view and z–y the top view. **A–C** represent Fcε3–4 in the 'vertical' orientation, **D–F** the 'horizontal', and **G–I** the 'front-back' orientation. The Fcε3–4 axes are shown for each view together with the corresponding axes of sFcεRI $\alpha$ . The *dotted outline* shows the path traced out by the centre of mass of sFcεRI $\alpha$  for a non-overlapping complex

**Table 2** Search ranges and number of models associated with each of the three translational searches are defined. The translations were performed in 0.5 nm steps

	x range	y range	z range	Total
	(nm)	(nm)	(nm)	models
Vertical Horizontal Front-back	-8.0  to  +8.0	-5.0 to +5.0 -6.0 to +6.0 -5.0 to +5.0	-4.0 to $+4.0$	13 209 14 025 13 125

## Systematic translational searches

A series of INSIGHT II (Biosym Technologies, Inc.) macros were developed, based on the AUTOSCT package (Beavil et al. 1995), and these were used to explore three degrees of translational freedom between the two elements of the complex.  $sFc \in RI\alpha$  was driven along its axes in a concerted stepwise manner by a series of nested loops within the macro scripts to generate many thousands of models. Taking the origin as when both centres of mass are superimposed, sFc $\varepsilon$ RI $\alpha$  was translated in steps of 0.5 nm along its own x, y and z axes such that it traced out a threedimensional grid (search grid), the dimensions of which were varied according to the orientation of Fc $\varepsilon$ 3–4. Fc $\varepsilon$ 3–4 was placed in one of three orientations. The first (referred to as vertical) consists of both sFc $\varepsilon$ RI $\alpha$  and Fc $\varepsilon$ 3–4 sharing identically aligned long (x) axes. The second (horizontal) has Fc $\varepsilon$ 3–4 lying at 90° following a +90° rotation about its z axis. The third (front-back) has a rotation of +90° about the y axis. The models are shown in Fig. 1, and Table 2 shows the translational range and the number of models associated with each of the three translational searches.

#### **Results**

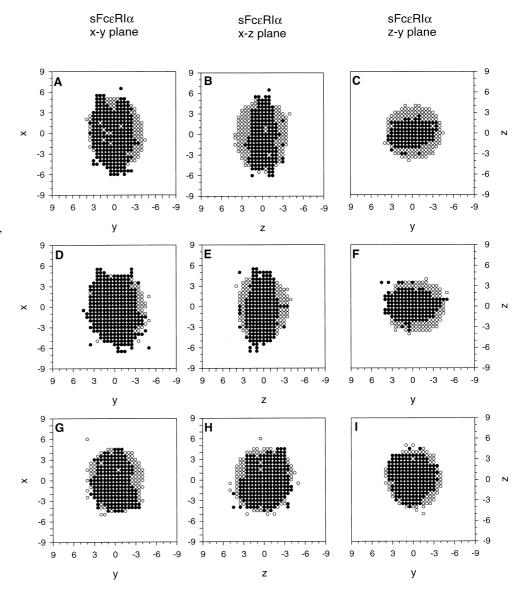
The sphere models generated are an accurate representation of the complex

The sphere models generated for  $Fc\varepsilon 3-4$  and  $sFc\varepsilon RI\alpha$  were used to calculate sedimentation coefficients. Both of these were within 0.1 S of the experimental values (Table 3), indicating the individual models for  $Fc\varepsilon 3-4$  and  $sFc\varepsilon RI\alpha$  were accurate representations of each protein. The models for the complexes were examined and it was found that in a non-overlapping complex the volume varied (Table 1), but was never underestimated by more than

**Table 3** Sedimentation coefficients determined experimentally or calculated from models of  $Fc\varepsilon 3-4$ ,  $sFc\varepsilon RI\alpha$  and their complex

	Experimental $s_{20,w}^0(S)$	Calculated $s_{20,w}^0(S)$
Fc $\varepsilon$ 3–4	$3.77 \pm 0.05$	3.85
sFc $\varepsilon$ RI $\alpha$	$2.80 \pm 0.05$	2.73
Complex	$4.95 \pm 0.05$	3.4 to 6.4

Fig. 2A-I Scatter plots of the  $Fc\varepsilon 3-4/sFc\varepsilon RI\alpha$  complex models. Models are viewed projected onto orthogonal planes defined by the axes of sFc $\varepsilon$ RI $\alpha$  (as in Fig. 1) with dimensions of nm. The solid dots represent the models with between 360-370 spheres and essentially define the shape of Fc $\varepsilon$ 3–4. The *hollow dots* represent models with a calculated  $s_{20,w}^0$  within  $\pm 0.1S$  of the experimentally observed value, and define which surfaces of Fc $\varepsilon$ 3–4 may be occupied by  $sFc \in RI\alpha$  within the complex. The interpretation of these data, in terms of which faces of Fc $\varepsilon$ 3–4 are available for binding sFc $\varepsilon$ RI $\alpha$ , is given in Table 4



3.5%, depending upon the orientation and this has no significant effect on the calculated frictional coefficients.

## Visual interpretation of the data

Table 3 shows the experimentally derived sedimentation coefficients for the complex and its two components together with the corresponding results from the models. Interpreting the data from 40,359 models is far from a trivial task. We have chosen to display the data in the form of a scatter plot (Fig. 2) which shows orthogonal views of the complex projected onto three planes from each of the three possible orientations for Fc $\varepsilon$ 3–4, namely, (in terms of the axes of sFc $\varepsilon$ RI $\alpha$  which remain invariant throughout), the x-y plane (front view), the x-z plane (side view) and the z-y plane (top view). Figure 1 shows schematically the orientation of the two components of the complex in each

of the panels in Fig. 2. In looking at the data, there are several things which must be considered. To a first approximation, the filled circles define the outline of the Fc $\varepsilon$ 3–4 and the open circles delimit the regions of the surface that sFc $\varepsilon$ RI $\alpha$  may inhabit. The filled circles represent models with between 360 and 370 spheres inclusive and the open circles represent models with more than 370 spheres (i.e., minimal overlap) but with a sedimentation coefficient within a fixed range of the experimental value for the complex of  $\pm 0.1$ S. If no overlap occurs between the two component models when they are in the search grid before the spheres are assigned, 401 spheres should appear in the sphere model although spurious effects related to the precise orientation of the molecular model within the search grid give rise to small fluctuations in the number of spheres. Overlap between the models results in a reduction of the number of spheres. We have used a loss of around 5% of the spheres as indicating the beginning of overlap i.e. 380 spheres or less. The decision to represent  $Fc\varepsilon 3-4$  by those models with between 360 and 370 spheres is an arbitrary one. When set at 370, the representations give a more interpretable outline to  $Fc\varepsilon 3-4$ .

Whilst considering the shape of Fc $\varepsilon$ 3–4, it should be noted that rather than define the surface of Fc $\varepsilon$ 3–4, the filled circles actually trace out the centre of mass of sFc $\varepsilon$ RI $\alpha$ . The consequence of this is that if sFc $\varepsilon$ RI $\alpha$  approaches  $Fc\varepsilon 3-4$  'end on', it will begin to overlap further from the surface that if it approaches 'side on' (one domain length as opposed to half a domain width). As an example, consider panels C and G which from the schematic diagram would be expected to have the same shape, but look quite different as sphere models. The dotted lines in the schematic diagram show the expected shape distortion for each orientation. In addition, the representations shown in Fig. 2 are asymmetrical. This is a reflection of the fact that the sFc $\varepsilon$ RI $\alpha$  model used is asymmetric, having a bend between the two immunoglobulin domains, and also having an uneven glycosylation profile (McDonnell et al. 1996).

## Comparison with experimental data

Table 4 shows a summary of the each of the panels in Fig. 2. We have considered the possibility of  $sFc\varepsilon RI\alpha$  approaching the flat face, sides and ends of  $Fc\varepsilon 3-4$  in all of the possible orientations, and we have indicated whether each position is possible, marginal or excluded. In each case, one of the approaches does not apply, as the data in every panel represents the movement of  $sFc\varepsilon RI\alpha$  using only two of the axes, to enable two-dimensional representation of the data. There is also some overlap between models, as some of the extreme configurations occur in more than one panel, but this serves to strengthen any conclusions drawn. In summary, if the long axis of  $sFc\varepsilon RI\alpha$  is parallel to the long axis of  $Fc\varepsilon 3-4$ , i.e. vertical (panels A, B and C), it is clear that the  $sFc\varepsilon RI\alpha$  can sit on the flat face or sides of  $Fc\varepsilon 3-4$ , but not on the bottom, and probably

**Table 4** Interpretation of the data shown in Fig. 2, indicating which faces of  $Fc\varepsilon 3-4$  are available for binding  $sFc\varepsilon RI\alpha$ . An indication of the level of confidence in the prediction is given by either Yes, No or Marginal, and where possible to which end of  $Fc\varepsilon 3-4$  the prediction belongs

	x-y plane	x-z plane	z-y plane
Vertical (A, B, C)	Flat: N/A Sides: Yes Ends: Marginal (Top)	Flat: Yes Sides: N/A Ends: No	Flat: Yes Sides: Marginal Ends: N/A
Horizontal (D, E, F)	Flat: N/A Sides: No Ends: Marginal (Top)	Flat: Yes Sides: No Ends: N/A	Flat: Yes Sides: N/A Ends: Marginal (Top)
Front-back (G, H, I)	Flat: Marginal Sides: Yes Ends: N/A	Flat: Marginal Sides: N/A Ends: Yes	Flat: N/A Sides: Yes Ends: Marginal

not on the top. If, however, the long axis of  $\text{sFc} \in \text{RI} \alpha$  is perpendicular to the long axis of  $\text{Fc} \in \text{3-4}$  (horizontal) as shown in panels D, E and F,  $\text{sFc} \in \text{RI} \alpha$  can occupy the flat face, and possibly the top, but the bottom and sides are excluded. The last set of models, G, H and I, with  $\text{sFc} \in \text{RI} \alpha$  end on to the flat face of  $\text{Fc} \in \text{3-4}$  (front-back), indicate that  $\text{sFc} \in \text{RI} \alpha$  in this orientation can occupy the flat face, and possibly the sides and ends. From this information, it is clear that only the more compact models are compatible with the experimental data, and elongated models are ruled out.

#### **Discussion**

The aim of this study was to analyse the Fc $\varepsilon$ 3–4/sFc $\varepsilon$ RI $\alpha$ complex more thoroughly than had previously been attempted. It has led to the creation of an automated method for easily generating large numbers of models, in this case 40,359, and comparing them all to experimentally determined sedimentation coefficients. Despite any possible objections based on uncertainty in the quantity of hydration associated with the hydrodynamic models, the precision associated with the agreement of calculated sedimentation coefficients with experimental data has been calibrated by Perkins (1993) and shown to be on average close to  $\pm 0.1$ S. The sedimentation coefficients we have calculated for Fc $\varepsilon$ 3–4 and sFc $\varepsilon$ RI $\alpha$  alone fall within this range (Table 3). We have used this as a cut off value to analyse the models we have produced, although less restrictive cut off values up to  $\pm 0.3$ S yield similar results (data not shown).

The results obtained are more rigorous than those presented in Keown et al. 1995 for the IgE-Fc/sFc $\varepsilon$ RI $\alpha$ complex, and although it is impossible to define the IgE/sFc $\varepsilon$ RI $\alpha$  interaction precisely, the results presented in Fig. 2 and Table 4 indicate that many binding configurations can be ruled out. It appears that the interaction between Fc $\varepsilon$ 3–4 and sFc $\varepsilon$ RI $\alpha$  is fairly compact, as elongated models are not compatible with the experimental data. It also suggests that sFc $\varepsilon$ RI $\alpha$  is unlikely to be interacting with the bottom of Fc $\varepsilon$ 3–4, and probably lies either along the sides or on the flat face. This is consistent with other experimental data on sFc $\varepsilon$ RI $\alpha$  binding to IgE and its recombinant fragments. It is known that domain 2 of sFc $\varepsilon$ RI $\alpha$  (Nissim and Eshhar 1992; Basu et al. 1993; Robertson 1993; Scarselli et al. 1993; reviewed in Hulett and Hogarth 1994) binds to the C&3 domains of IgE (Helm et al. 1988; Nissim and Eshhar 1992; Basu et al. 1993; reviewed in Sutton and Gould 1993 and Beavil et al. 1993), which confirms the fact that  $sFc \in RI\alpha$  cannot lie along the bottom of Fc $\varepsilon$ 3–4. As domain 2 of sFc $\varepsilon$ RI $\alpha$  is the membrane-proximal domain in the native protein, it is also unlikely that it is able to bind 'end-on' to IgE: this is confirmed by the fact that models where sFc $\varepsilon$ RI $\alpha$  interacts 'end-on' with the Fc $\varepsilon$ 3–4 are not compatible with the experimentally determined sedimentation coefficients. This study could not determine whether binding was on the sides or face of Fc $\varepsilon$ 3–4, however.

The calculations performed in this study took the equivalent of nine days of CPU time on 100 MHz Silicon Graphics Indy R4000SC UNIX workstations. In fact, the method is very amenable to parallel processing techniques, and the whole exercise was completed over a single weekend, once set up, by splitting the tanks and running it concurrently on three identical workstations. The hydrodynamic calculations were performed using GENDIA rather than HYDRO (Garcia de la Torre et al. 1994) because of the relative difference in speed, which is almost an order of magnitude. However, development of a small dedicated program for manipulating the molecular models, rather than the use of Insight II, combined with a tighter integration of the other functions could easily generate a speed increase sufficient to make the use of the more rigorous program HYDRO a practical proposition. The use of HYDRO would also enable a number of additional hydrodynamic parameters such as intrinsic viscosity, translational diffusion coefficients and rotational relaxation times to be included as additional constraining factors. Any other constraints to the model are easily incorporated in the calculations, and this may include data from a wide variety of sources such as X-ray or neutron scattering studies (for example, see Beavil et al. 1995). This kind of automated modelling is feasible for anyone with an entry-level workstation, and could be further developed, for example using Monte Carlo methods. It should certainly be considered by anyone studying a reasonably elongated high affinity complex.

Because this method uses models based on the known structure of domains, it is more specific than other methods which model proteins as simple geometric shapes. Whilst it is still not possible to analyse the experimental data so as to arrive at a unique structure which fits the data, given a range of models, it is possible to filter out implausible structures. The more filters that can be applied to the agreement between the models and the experimental data, the more confidence one can have in the limits that are defined by the modelling procedure. In many applications it should be possible to arrive at a very limited range of models which fit both the experimental data and the constraints known to apply to the structure.

The automated hydrodynamic modelling method described here clearly has the potential to define the limits of interactions between the components of a complex in a far more thorough way than has been possible in the past. In the future, it will be essential to undertake a rigorous examination and calibration of the limits of the calculations. This technique has the benefits of being automatic, once the axes of the two components have been defined, and enables all possible orientations of the components relative to one another to be investigated. Conventional modelling techniques, where each complex is built by hand do not feasibly allow such a thorough study to be carried out, so the application of this technique represents a significant advance in the study of complex formation using hydrodynamic methods.

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